

# Units, and Unit Conversion

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## I. Lengths

### a) Metric lengths

- 1) Complete the following set of conversion factors, relative to the metre. Use index form for any factors smaller than 0.01 or greater than 100; otherwise use decimals.

				SI prefix			
<b>1 pm</b>	=	<b>10<sup>-12</sup></b>	<b>m</b>	<b>pico</b>	_____	<b>pm</b>	= <b>1 m</b>
1 Å	=	10 <sup>-10</sup>	m	–	10 <sup>+10</sup>	Å	= 1 m
<b>1 nm</b>	=	_____	<b>m</b>	<b>nano</b>	_____	<b>nm</b>	= <b>1 m</b>
<b>1 µm</b>	=	_____	<b>m</b>	<b>micro</b>	_____	<b>µm</b>	= <b>1 m</b>
<b>1 mm</b>	=	_____	<b>m</b>	<b>milli</b>	_____	<b>mm</b>	= <b>1 m</b>
1 cm	=	_____	m	centi	_____	cm	= 1 m
1 dm	=	0.1	m	deci	10	dm	= 1 m
<b>1 m</b>	=	_____	<b>m</b>	–	_____	<b>m</b>	= <b>1 m</b>
1 hm	=	100	m	hecto	0.01	hm	= 1 m
<b>1 km</b>	=	_____	<b>m</b>	<b>kilo</b>	_____	<b>km</b>	= <b>1 m</b>

Notice that for the rows in bold the conversion factors can be written as ten raised to a multiple of three.

Ångströms (Å) are occasionally used for measurements of atom, ion and molecule sizes. Decimetres (dm) can be used as the basis for the litre (L). Hectometres (hm) are conveniently referred to as a *memory aid* when working with the hectare (ha).

- 2) Complete the following set of conversion factors. Use index form for any factors smaller than 0.01 or greater than 100; otherwise use decimals.

EXAMPLE:  $1 \text{ \AA} = ? \text{ pm}$ .

From the preceding exercise you can read conversion factors of  $10^{-10} \text{ m/\AA}$ , and  $10^{+12} \text{ pm/m}$ . Thus,  $1 \text{ \AA} = (1 \times 10^{-10}) \text{ m} = 10^{-10} \text{ m} = (10^{-10} \times 10^{+12}) \text{ pm} = 100 \text{ pm}$ .

1	pm	=	_____	nm	_____	pm	=	1	$\mu\text{m}$
1	$\text{\AA}$	=	100	pm	10	$\text{\AA}$	=	1	nm
1	nm	=	_____	$\mu\text{m}$	_____	nm	=	1	pm
1	$\mu\text{m}$	=	_____	mm	_____	$\mu\text{m}$	=	1	cm
1	mm	=	_____	km	_____	mm	=	1	$\text{\AA}$
1	cm	=	_____	dm	_____	cm	=	1	km
1	dm	=	$10^{+5}$	$\mu\text{m}$	0.01	dm	=	1	mm
1	m	=	_____	nm	_____	m	=	1	$\mu\text{m}$
1	km	=	_____	cm	_____	km	=	1	nm

- 3) Find the equivalent length. Use scientific notation for any values smaller than 0.01 or greater than 100; otherwise use decimals.

EXAMPLE:  $0.8 \text{ dm} = ? \text{ nm}$ .

From the first exercise you can read conversion factors of  $10^{-1} \text{ m/dm}$ , and  $10^{+9} \text{ nm/m}$ . Thus,  $0.8 \text{ dm} = (0.8 \times 10^{-1}) \text{ m} = 8 \times 10^{-2} \text{ m} = (8 \times 10^{-2} \times 10^{+9}) \text{ nm} = 8 \times 10^{+7} \text{ nm}$ .

7	pm	=	_____	mm	_____	pm	=	8	$\text{\AA}$
8	$\text{\AA}$	=	_____	$\mu\text{m}$	_____	$\text{\AA}$	=	4	km
5	nm	=	_____	mm	_____	nm	=	4	mm
3	$\mu\text{m}$	=	_____	km	_____	$\mu\text{m}$	=	7	mm
95	mm	=	_____	dm	_____	mm	=	83	nm
28	cm	=	_____	$\mu\text{m}$	_____	cm	=	55	dm
0.8	dm	=	$8 \times 10^{+7}$	nm	_____	dm	=	0.39	nm
0.04	m	=	_____	cm	$9.1 \times 10^{-11}$	m	=	91	pm
0.4	km	=	_____	nm	_____	km	=	22	cm

## b) Imperial lengths

4) Complete the following set of conversion factors. Use decimal form.

1	foot	=	12	inches	24	furlongs	=	1	league
1	yard	=	3	feet	_____	inches	=	1	yard
1	furlong	=	220	yards	_____	inches	=	1	furlong
1	mile	=	8	furlongs	_____	inches	=	1	mile
1	league	=	3	miles	_____	inches	=	1	league
					_____	yards	=	1	mile

5) Complete the following set of conversion factors. Use decimal notation.

1	inch	=	25.4	mm	_____	mm	=	1	foot
					_____	cm	=	1	foot
1	mile	=	_____	mm	_____	m	=	1	foot
1	mile	=	_____	cm	_____	$\mu\text{m}$	=	1	yard
1	mile	=	_____	m	_____	mm	=	1	yard
1	mile	=	1.609344	km	_____	m	=	1	yard

6) Find the equivalent length. Use scientific notation for any values smaller than 0.01 or greater than 100; otherwise use decimals.

3	inches	=	76.2	mm	$2.1336 \times 10^9$	nm	=	7	feet
4	inches	=	_____	cm	_____	cm	=	9	feet
51	inches	=	_____	km	_____	$\mu\text{m}$	=	12	feet
24	inches	=	_____	cm	_____	mm	=	5.5	feet
47	inches	=	_____	m	_____	m	=	101	yards
600	inches	=	_____	km	_____	m	=	0.2	miles

## II. Areas

Areas are obtained by *multiplying two lengths*. Therefore the units of area are commonly the **square** of a unit of length — although some special names are also defined.

- 7) Complete the following set of conversion factors, relative to the square metre. Use scientific notation for any values smaller than 0.01 or greater than 100; otherwise use decimals.

				SI prefix				
<b>1 pm<sup>2</sup></b>	=	<b>10<sup>-24</sup></b>	<b>m<sup>2</sup></b>	—	_____	<b>pm<sup>2</sup></b>	=	<b>1 m<sup>2</sup></b>
<b>1 nm<sup>2</sup></b>	=	_____	<b>m<sup>2</sup></b>	—	<b>10<sup>+18</sup></b>	<b>nm<sup>2</sup></b>	=	<b>1 m<sup>2</sup></b>
<b>1 μm<sup>2</sup></b>	=	_____	<b>m<sup>2</sup></b>	—	_____	<b>μm<sup>2</sup></b>	=	<b>1 m<sup>2</sup></b>
<b>1 mm<sup>2</sup></b>	=	_____	<b>m<sup>2</sup></b>	—	_____	<b>mm<sup>2</sup></b>	=	<b>1 m<sup>2</sup></b>
1 cm <sup>2</sup>	=	_____	m <sup>2</sup>	—	_____	cm <sup>2</sup>	=	1 m <sup>2</sup>
<b>1 m<sup>2</sup></b>	=	<b>1</b>	<b>m<sup>2</sup></b>	—	_____	<b>m<sup>2</sup></b>	=	<b>1 m<sup>2</sup></b>
1 a	=	100	m <sup>2</sup>	—	0.01	a	=	1 m <sup>2</sup>
1 ha	=	10 <sup>4</sup>	m <sup>2</sup>	hecto	_____	ha	=	1 m <sup>2</sup>
<b>1 km<sup>2</sup></b>	=	_____	<b>m<sup>2</sup></b>	—	_____	<b>km<sup>2</sup></b>	=	<b>1 m<sup>2</sup></b>

For units of area based on squaring a unit of distance, the conversion factors for distance are simply squared.

For example:

$$10 \text{ mm} = 1 \text{ cm}$$

$$(10 \text{ mm})^2 = (1 \text{ cm})^2$$

$$10^2 \text{ mm}^2 = 1^2 \text{ cm}^2$$

$$100 \text{ mm}^2 = 1 \text{ cm}^2$$

Note that the SI prefix has priority over any mathematical operations. Thus, “cm<sup>2</sup>” means “the square of a centimetre”; it does not mean “a one-hundredth of a square metre”.

Notice that for the rows in bold the conversion factors can be written as ten raised to a multiple of six (2×3).

“a” represents the “are”, an uncommon unit of area equal to 100 m<sup>2</sup> — *e.g.* a square of size 10 m × 10 m.

“ha” represents the “hectare” a common unit of area equal to 10000 m<sup>2</sup> — *e.g.* a square of size 100 m × 100 m (*coincidentally* equivalent to a square of size 1 hm × 1 hm).

- 8) Complete the following set of conversion factors. Use index form for any factors smaller than 0.01 or greater than 100; otherwise use decimals.

EXAMPLE:  $1 \text{ pm}^2 = ? \text{ ha}$ .

From the preceding exercise you can read conversion factors of  $10^{-24} \text{ m}^2/\text{pm}^2$ , and  $10^{-4} \text{ ha}/\text{m}^2$ . Thus,  $1 \text{ pm}^2 = (1 \times 10^{-24}) \text{ m}^2 = 10^{-24} \text{ m}^2 = (10^{-24} \times 10^{-4}) \text{ ha} = 10^{-28} \text{ ha}$ .

1	$\text{pm}^2$	=	$10^{-28}$	ha	_____	$\text{pm}^2$	=	1	$\text{mm}^2$
1	$\text{nm}^2$	=	_____	$\text{km}^2$	_____	$\text{nm}^2$	=	1	$\text{cm}^2$
1	$\mu\text{m}^2$	=	_____	$\text{nm}^2$	_____	$\mu\text{m}^2$	=	1	ha
1	$\text{mm}^2$	=	_____	$\mu\text{m}^2$	_____	$\text{mm}^2$	=	1	$\text{mm}^2$
1	$\text{cm}^2$	=	_____	$\text{mm}^2$	_____	$\text{cm}^2$	=	1	ha
1	$\text{m}^2$	=	_____	$\text{cm}^2$	_____	$\text{m}^2$	=	1	$\text{mm}^2$
1	a	=	0.01	ha	$10^{+4}$	a	=	1	$\text{km}^2$
1	ha	=	_____	$\text{mm}^2$	_____	ha	=	1	$\text{nm}^2$
1	$\text{km}^2$	=	_____	ha	_____	$\text{km}^2$	=	1	$\mu\text{m}^2$

- 9) Find the equivalent area. Use scientific notation for any values smaller than 0.01 or greater than 100; otherwise use decimals.

5	$\text{pm}^2$	=	_____	ha	_____	$\text{pm}^2$	=	9	$\text{nm}^2$
3	$\text{nm}^2$	=	_____	$\text{mm}^2$	_____	$\text{nm}^2$	=	2	$\mu\text{m}^2$
9	$\mu\text{m}^2$	=	_____	ha	_____	$\mu\text{m}^2$	=	8	$\text{mm}^2$
2	$\text{mm}^2$	=	_____	ha	_____	$\text{mm}^2$	=	0.04	$\text{cm}^2$
7	$\text{cm}^2$	=	_____	$\text{km}^2$	_____	$\text{cm}^2$	=	0.4	ha
15	$\text{m}^2$	=	_____	$\text{nm}^2$	_____	$\text{m}^2$	=	77	$\text{mm}^2$
30	a	=	$3.0 \times 10^{+15}$	$\mu\text{m}^2$	_____	a	=	30	ha
0.15	ha	=	_____	$\text{mm}^2$	_____	ha	=	500	$\text{cm}^2$
401	$\text{km}^2$	=	_____	$\text{cm}^2$	_____	$\text{km}^2$	=	58	$\text{pm}^2$

### III. Volumes

Volumes are obtained by *multiplying three lengths*. Therefore the units of volume are commonly the **cube** of a unit of length — although several special names are also defined.

#### a) Based on cubing units of distance

10) Complete the following set of conversion factors, relative to the cubic metre. Use scientific notation for any values smaller than 0.01 or greater than 100; otherwise use decimals.

<b>1 pm<sup>3</sup></b>	=	_____	<b>m<sup>3</sup></b>	<b>10<sup>+36</sup></b>	<b>pm<sup>3</sup></b>	=	<b>1 m<sup>3</sup></b>
<b>1 nm<sup>3</sup></b>	=	_____	<b>m<sup>3</sup></b>	_____	<b>nm<sup>3</sup></b>	=	<b>1 m<sup>3</sup></b>
<b>1 μm<sup>3</sup></b>	=	_____	<b>m<sup>3</sup></b>	_____	<b>μm<sup>3</sup></b>	=	<b>1 m<sup>3</sup></b>
<b>1 mm<sup>3</sup></b>	=	_____	<b>m<sup>3</sup></b>	_____	<b>mm<sup>3</sup></b>	=	<b>1 m<sup>3</sup></b>
1 cm <sup>3</sup>	=	_____	m <sup>3</sup>	_____	cm <sup>3</sup>	=	1 m <sup>3</sup>
1 dm <sup>3</sup>	=	_____	m <sup>3</sup>	_____	dm <sup>3</sup>	=	1 m <sup>3</sup>
<b>1 m<sup>3</sup></b>	=	_____	<b>m<sup>3</sup></b>	_____	<b>m<sup>3</sup></b>	=	<b>1 m<sup>3</sup></b>
1 hm <sup>3</sup>	=	10 <sup>+6</sup>	m <sup>3</sup>	_____	hm <sup>3</sup>	=	1 m <sup>3</sup>
<b>1 km<sup>3</sup></b>	=	_____	<b>m<sup>3</sup></b>	_____	<b>km<sup>3</sup></b>	=	<b>1 m<sup>3</sup></b>

For units of volume based on cubing a unit of distance, the conversion factors for distance are simply cubed.

For example:

$$10 \text{ mm} = 1 \text{ cm}$$

$$(10 \text{ mm})^3 = (1 \text{ cm})^3$$

$$10^3 \text{ mm}^3 = 1^3 \text{ cm}^3$$

$$1000 \text{ mm}^3 = 1 \text{ cm}^3$$

Note that the SI prefix has priority over any mathematical operations. Thus, “cm<sup>3</sup>” means “the cube of a centimetre”; it does not mean “a one-hundredth of a cubic metre”.

Notice that for the rows in bold the conversion factors can be written as ten raised to a multiple of nine (3×3).

“hm” represents the “hectometre” an uncommon unit of length (equal to 100 m) that is seldom used in relation to volumes.

- 11) Complete the following set of conversion factors. Use index form for any factors smaller than 0.01 or greater than 100; otherwise use decimals.

1	pm <sup>3</sup>	=	_____	dm <sup>3</sup>	10 <sup>+27</sup>	pm <sup>3</sup>	=	1	mm <sup>3</sup>
1	nm <sup>3</sup>	=	_____	km <sup>3</sup>	_____	nm <sup>3</sup>	=	1	cm <sup>3</sup>
1	µm <sup>3</sup>	=	_____	nm <sup>3</sup>	_____	µm <sup>3</sup>	=	1	dm <sup>3</sup>
1	mm <sup>3</sup>	=	_____	µm <sup>3</sup>	_____	mm <sup>3</sup>	=	1	mm <sup>3</sup>
1	cm <sup>3</sup>	=	_____	mm <sup>3</sup>	_____	cm <sup>3</sup>	=	1	dm <sup>3</sup>
1	dm <sup>3</sup>	=	_____	cm <sup>3</sup>	_____	dm <sup>3</sup>	=	1	mm <sup>3</sup>
1	m <sup>3</sup>	=	_____	dm <sup>3</sup>	_____	m <sup>3</sup>	=	1	km <sup>3</sup>
1	hm <sup>3</sup>	=	10 <sup>+15</sup>	mm <sup>3</sup>	_____	hm <sup>3</sup>	=	1	nm <sup>3</sup>
1	km <sup>3</sup>	=	_____	dm <sup>3</sup>	_____	km <sup>3</sup>	=	1	µm <sup>3</sup>

- 12) Find the equivalent volume. Use scientific notation for any values smaller than 0.01 or greater than 100; otherwise use decimals.

2	pm <sup>3</sup>	=	_____	dm <sup>3</sup>	_____	pm <sup>3</sup>	=	3	nm <sup>3</sup>
8	nm <sup>3</sup>	=	_____	mm <sup>3</sup>	_____	nm <sup>3</sup>	=	5	µm <sup>3</sup>
9	µm <sup>3</sup>	=	_____	dm <sup>3</sup>	_____	µm <sup>3</sup>	=	10	mm <sup>3</sup>
51	mm <sup>3</sup>	=	_____	dm <sup>3</sup>	_____	mm <sup>3</sup>	=	100	cm <sup>3</sup>
82	cm <sup>3</sup>	=	_____	km <sup>3</sup>	_____	cm <sup>3</sup>	=	0.2	dm <sup>3</sup>
110	dm <sup>3</sup>	=	_____	nm <sup>3</sup>	_____	dm <sup>3</sup>	=	12	mm <sup>3</sup>
567	m <sup>3</sup>	=	_____	µm <sup>3</sup>	_____	m <sup>3</sup>	=	60	dm <sup>3</sup>
0.66	hm <sup>3</sup>	=	_____	mm <sup>3</sup>	7.07×10 <sup>-10</sup>	hm <sup>3</sup>	=	707	cm <sup>3</sup>
66	km <sup>3</sup>	=	_____	cm <sup>3</sup>	_____	km <sup>3</sup>	=	0.01	pm <sup>3</sup>

## b) Based on litres

- 13) Complete the following set of conversion factors, relative to the litre. Use scientific notation for any values smaller than 0.01 or greater than 100; otherwise use decimals.

				SI prefix			
<b>1 pL</b>	=	<b>10<sup>-12</sup></b>	<b>L</b>	<b>pico</b>	_____	<b>pL</b>	= <b>1 L</b>
<b>1 nL</b>	=	_____	<b>L</b>	<b>nano</b>	_____	<b>nL</b>	= <b>1 L</b>
<b>1 µL</b>	=	_____	<b>L</b>	<b>micro</b>	_____	<b>µL</b>	= <b>1 L</b>
<b>1 mL</b>	=	_____	<b>L</b>	<b>milli</b>	_____	<b>mL</b>	= <b>1 L</b>
1 cL	=	0.01	L	centi	_____	cL	= 1 L
1 dL	=	_____	L	deci	10	dL	= 1 L
<b>1 L</b>	=	_____	<b>L</b>	–	_____	<b>L</b>	= <b>1 L</b>
1 hL	=	100	L	hecto	_____	hL	= 1 L
<b>1 kL</b>	=	_____	<b>L</b>	<b>kilo</b>	_____	<b>kL</b>	= <b>1 L</b>
<b>1 ML</b>	=	_____	<b>L</b>	<b>mega</b>	_____	<b>ML</b>	= <b>1 L</b>
<b>1 GL</b>	=	_____	<b>L</b>	<b>giga</b>	<b>10<sup>-9</sup></b>	<b>GL</b>	= <b>1 L</b>

Notice that for the rows in bold the conversion factors can be written as ten raised to a multiple of three.

The units not listed in bold are less commonly used.

- 14) Complete the following set of conversion factors. Use index form for any factors smaller than 0.01 or greater than 100; otherwise use decimals.

1 pL	=	10 <sup>-9</sup>	mL	_____ pL	=	1	µL
1 nL	=	_____	kL	_____ nL	=	1	mL
1 µL	=	_____	ML	_____ µL	=	1	pL
1 mL	=	_____	kL	_____ mL	=	1	nL
1 cL	=	_____	pL	10 cL	=	1	dL
1 dL	=	10 <sup>+8</sup>	nL	_____ dL	=	1	cL
1 L	=	_____	µL	_____ L	=	1	ML
1 hL	=	_____	µL	10 <sup>-5</sup> hL	=	1	mL
1 kL	=	_____	mL	_____ kL	=	1	GL
1 ML	=	_____	GL	_____ ML	=	1	mL
1 GL	=	_____	ML	_____ GL	=	1	kL



- 15) Find the equivalent volume. Use scientific notation for any values smaller than 0.01 or greater than 100; otherwise use decimals.

7	pL	=	_____	mL	$2 \times 10^{+18}$	pL	=	2	ML
6	nL	=	_____	kL	_____	nL	=	5	mL
4	$\mu$ L	=	_____	mL	_____	$\mu$ L	=	9	kL
12	mL	=	_____	nL	_____	mL	=	0.1	ML
5.5	cL	=	0.55	dL	_____	cL	=	0.5	mL
36	dL	=	_____	mL	_____	dL	=	654	L
70	L	=	_____	$\mu$ L	_____	L	=	0.03	nL
1.5	kL	=	_____	GL	_____	kL	=	128	$\mu$ L
80	ML	=	$8.0 \times 10^{+4}$	kL	_____	ML	=	50	GL
0.01	GL	=	_____	ML	_____	GL	=	5.8	kL

### c) Combination

One litre is equal to one cubic decimetre. Thus, a cube of side length 1 dm (*i.e.* 0.1 m) has a volume of one litre.

Hence, one cubic metre is equivalent to one thousand litres.

- 16) Complete the following set of conversion factors. Use index form for any factors smaller than 0.01 or greater than 100; otherwise use decimals.

1	$\text{pm}^3$	=	_____	L	1	$\text{dm}^3$	=	1	L
1	$\text{nm}^3$	=	_____	L	1	$\text{m}^3$	=	$10^{+3}$	L
1	$\mu\text{m}^3$	=	_____	L	1	$\text{hm}^3$	=	_____	L
1	$\text{mm}^3$	=	_____	L	1	$\text{km}^3$	=	_____	L
1	$\text{cm}^3$	=	_____	L					

- 17) Complete the following set of conversion factors. Use index form for any factors smaller than 0.01 or greater than 100; otherwise use decimals.

**EXAMPLE:**  $1 \text{ nm}^3 = ? \text{ nL}$ .

Conversion factors of  $10^{-27}$  m<sup>3</sup>/nm<sup>3</sup>,  $10^{+3}$  L/m<sup>3</sup>, and  $10^{+9}$  nL/L can be applied.

$$\begin{aligned} 1 \text{ nm}^3 &= (1 \times 10^{-27}) \cancel{\text{nm}^3} \times \text{m}^3 / \cancel{\text{nm}^3} &&= 10^{-27} \text{ m}^3 \\ &= (10^{-27} \times 10^3) \cancel{\text{m}^3} \times \text{L} / \cancel{\text{m}^3} &&= 10^{-24} \text{ L} \\ &= (10^{-24} \times 10^9) \cancel{\text{L}} \times \text{nL} / \cancel{\text{L}} &&= 10^{-15} \text{ nL} . \end{aligned}$$

Notice that when the conversion factors are used in the correct sequence, the units will cancel appropriately in each step.

1	pm <sup>3</sup>	=	_____	pL	10 <sup>+42</sup>	pm <sup>3</sup>	=	1	GL
1	nm <sup>3</sup>	=	10 <sup>-15</sup>	nL	_____	nm <sup>3</sup>	=	1	cL
1	μm <sup>3</sup>	=	_____	kL	_____	μm <sup>3</sup>	=	1	dL
1	mm <sup>3</sup>	=	_____	μL	_____	mm <sup>3</sup>	=	1	mL
1	cm <sup>3</sup>	=	_____	mL	_____	cm <sup>3</sup>	=	1	dL
1	dm <sup>3</sup>	=	_____	ML	_____	dm <sup>3</sup>	=	1	mL
1	hm <sup>3</sup>	=	10 <sup>+12</sup>	mL	_____	m <sup>3</sup>	=	1	kL
1	km <sup>3</sup>	=		dL		hm <sup>3</sup>	=	1	nL

- 18) Find the equivalent volume. Use scientific notation for any values smaller than 0.01 or greater than 100; otherwise use decimals.

EXAMPLE:  $80 \text{ hm}^3 = ? \text{ ML}$ .

Conversion factors of  $10^6 \text{ m}^3/\text{hm}^3$ ,  $10^3 \text{ L}/\text{m}^3$ , and  $10^{-6} \text{ ML}/\text{L}$  apply.

$$\begin{aligned} 1 \text{ nm}^3 &= (80 \times 10^6) \cancel{\text{hm}^3} \times \cancel{\text{m}^3} / \cancel{\text{hm}^3} = 8 \times 10^7 \text{ m}^3 \\ &= (8 \times 10^7 \times 10^3) \cancel{\text{m}^3} \times \text{L} / \cancel{\text{m}^3} = 8 \times 10^{10} \text{ L} \\ &= (8 \times 10^{10} \times 10^{-6}) \cancel{\text{L}} \times \text{ML} / \cancel{\text{L}} = 8 \times 10^4 \text{ ML} . \end{aligned}$$

Notice that when the conversion factors are used in the correct sequence, the units will cancel appropriately in each step.

32	pm <sup>3</sup>	=	_____	pL	_____	dm <sup>3</sup>	=	33	ML
654	nm <sup>3</sup>	=	_____	nL	_____	mm <sup>3</sup>	=	10	mL
92	μm <sup>3</sup>	=	_____	μL	_____	dm <sup>3</sup>	=	8	kL
1.2	mm <sup>3</sup>	=	_____	mL	_____	dm <sup>3</sup>	=	98	ML
5.51	cm <sup>3</sup>	=	0.551	cL	_____	km <sup>3</sup>	=	18	mL
3	dm <sup>3</sup>	=	_____	dL	_____	nm <sup>3</sup>	=	2.2	L
700	m <sup>3</sup>	=	_____	L	_____	μm <sup>3</sup>	=	0.01	nL
1.05	m <sup>3</sup>	=	_____	hL	_____	mm <sup>3</sup>	=	0.05	μL
25	m <sup>3</sup>	=	_____	kL	_____	nm <sup>3</sup>	=	72	μL
80	hm <sup>3</sup>	=	8.0×10 <sup>+4</sup>	ML	_____	μm <sup>3</sup>	=	65	GL
9.01	km <sup>3</sup>	=	_____	GL	_____	mm <sup>3</sup>	=	11.1	kL

## IV. Time

19) Complete the following set of conversion factors. Use scientific notation for any values smaller than 0.01 or greater than 100; otherwise use decimals.

1 microsecond	= 1000	nanoseconds	_____ ns	= 1 s
1 millisecond	= 1000	microseconds	_____ $\mu$ s	= 1 d
1 second	= 1000	milliseconds	$3.6 \times 10^{+6}$ ms	= 1 h
1 minute	= 60	seconds	_____ s	= 1 d
1 hour	= 60	minutes	_____ min	= 1 d
1 day	= 24	hours	_____ h	= 1 week
1 week	= 7	days	_____ ns	= 1 ms
1 fortnight	= 14	days	_____ $\mu$ s	= 1 h
1 month	$\sim 30.4$	days	_____ ms	= 1 ns
1 month	$\sim 4$	weeks	_____ s	= 1 week
1 "year"	= 12	months	_____ min	= 1 fortnight
1 "year"	$\sim 365$	days	_____ h	= 1 week
1 solar year	$\approx 365.2422$	days	_____ $\mu$ s	= 1 min
1 sidereal year	$\approx 365.2564$	days	$1 \times 10^{-3}$ ms	= 1 $\mu$ s

The length of a "month" and a "year" varies. For maximum precision and to avoid ambiguity it is safer to avoid working in such units unless either (i) the situation demands it, (ii) a clear basis is stated, or (iii) only approximate, indicative values are needed.

20) Find the equivalent time. Use scientific notation for any values smaller than 0.01 or greater than 100; otherwise use decimals.

5 ms	= $5 \times 10^{+6}$	ns	_____ ns	= 7 h
8 min	_____ $\mu$ s		_____ $\mu$ s	= 9 min
58 min	= _____ ms		_____ ms	= 12 s
0.1 ns	= _____ s		_____ s	= 52 min
47 weeks	= _____ min		_____ min	= 101 h
47 weeks	= _____ h		_____ h	= 0.01 d
600 fortnights	= _____ d		_____ d	= 0.2 weeks

## V. Speed

Speed characterises distance travelled for a given duration.

21) Complete the following table.

For each pair of adjacent rows, write down the relevant length conversion factor.

For each pair of adjacent columns, write down the relevant time conversion factor.

		Time unit							Factor:
		ns	µs	ms	s	min	h	d	
Length unit	pm		$5.0 \times 10^9$	$5.0 \times 10^{12}$					
	nm								
	µm		$5.0 \times 10^3$						
	mm	$5.0 \times 10^{-3}$	5.0	$5.0 \times 10^3$	$5.0 \times 10^6$			$4.32 \times 10^{11}$	× 0.1
	cm		0.5		$5.0 \times 10^5$				
	dm		0.05						
	m		$5.0 \times 10^{-3}$						
	hm						$1.8 \times 10^5$		
	km		$5.0 \times 10^{-6}$						
Factor:			$\times 10^3$						

Explanation:

Start with  $5.0 \text{ mm}/\mu\text{s}$  (highlighted). To find the equivalent speed in  $\text{cm}/\text{s}$  use the relevant length and time conversion factors, namely  $0.1 \text{ cm}/\text{mm}$  and  $10^6 \mu\text{s}/\text{s}$ .

Writing the units in index form shows which numerical factor to use for consistency:

$$5.0 \text{ mm } \mu\text{s}^{-1} = 5.0 \text{ mm } \mu\text{s}^{-1} \times 0.1 \text{ cm mm}^{-1} \times 10^6 \mu\text{s s}^{-1}$$

$$5.0 \text{ mm } \mu\text{s}^{-1} = 5.0 \times 0.1 \text{ cm} \times 10^6 \text{ s}^{-1}$$

$$5.0 \text{ mm } \mu\text{s}^{-1} = 5.0 \times 0.1 \times 10^6 \text{ cm s}^{-1}$$

$$5.0 \text{ mm } \mu\text{s}^{-1} = 5.0 \times 10^5 \text{ cm s}^{-1}$$

Notice that  $\text{mm}$  cancels with  $\text{mm}^{-1}$ , while  $\mu\text{s}^{-1}$  cancels with  $\mu\text{s}$ .

The conversion would be inconsistent (and hence unsuccessful) if multiplication by  $10 \text{ mm}/\text{cm}$  or  $10^{-6} \text{ s}/\mu\text{s}$  were attempted here.

## VI. Concentration

Concentration can be expressed in various ways, including the mass of solute (*e.g.* salt) per volume of solution (*e.g.* seawater).

22) Complete the following table.

For each pair of adjacent rows, write down the relevant mass conversion factor.

For each pair of adjacent columns, write down the relevant volume conversion factor.

		Volume unit						Factor:
		$\mu\text{m}^3$	$\text{mm}^3$	$\mu\text{L}$	$\text{mL}$	$\text{L}$	$\text{m}^3$	$\text{GL}$
Mass unit	<b>pg</b>							
	<b>ng</b>							
	<b><math>\mu\text{g}</math></b>							
	<b>mg</b>	$8.7 \times 10^{-10}$	0.87		870			$\times$
	<b>cg</b>		0.087		87			0.1
	<b>g</b>							
	<b>kg</b>		$8.7 \times 10^{-7}$					
	<b>Mg</b>							
	<b>Gg</b>							
Factor:		$\times 10^{+9}$						

For large masses the tonne (t), kilotonne (kt) and megatonne (Mt) are more commonly employed than the megagram (Mg), gigagram (Gg) and teragram (Tg).

Explanation:

Start with  $0.87 \text{ mg/mm}^3$  (highlighted). To find the equivalent concentration in  $\text{cg/mL}$  use the relevant mass and volume conversion factors, namely  $0.1 \text{ cg/mg}$  and  $10^{+3} \text{ mm}^3/\text{mL}$ .

Writing the units in index form shows which numerical factor to use for consistency:

$$0.87 \text{ mg mm}^{-3} = 0.87 \text{ mg mm}^{-3} \times 0.1 \text{ cg mg}^{-1} \times 10^{+3} \text{ mm}^3 \text{ mL}^{-1}$$

$$0.87 \text{ mg mm}^{-3} = 0.87 \times 0.1 \text{ cg} \times 10^{+3} \text{ mL}^{-1}$$

$$0.87 \text{ mg mm}^{-3} = 0.87 \times 0.1 \times 10^{+3} \text{ cg mL}^{-1}$$

$$0.87 \text{ mg mm}^{-3} = 87 \text{ cg mL}^{-1}$$

Notice that  $\text{mg}$  cancels with  $\text{mg}^{-1}$ , while  $\text{mm}^{-3}$  cancels with  $\text{mm}^3$ .

## VII. Additional prefixes

The following SI prefixes are also defined.

Prefix	Symbol	Factor	Example:		
yocto	y	$10^{-24}$	$10^{-24}$ g	=	1 yg
zepto	z	$10^{-21}$	$10^{-21}$ g	=	1 zg
atto	a	$10^{-18}$	$10^{-18}$ g	=	1 ag
femto	f	$10^{-15}$	$10^{-15}$ g	=	1 fg
...				=	
deca	da	$10^{+1}$	$10^{+1}$ m	=	1 dam
...				=	
tera	T	$10^{+12}$	$10^{+12}$ J	=	1 TJ
peta	P	$10^{+15}$	$10^{+15}$ J	=	1 PJ
exa	E	$10^{+18}$	$10^{+18}$ J	=	1 GJ
zetta	Z	$10^{+21}$	$10^{+21}$ g	=	1 Zg
yotta	Y	$10^{+24}$	$10^{+24}$ g	=	1 Yg

Notice that most factors have an index that is a multiple of three.

Take care to distinguish “deca” (da) from “deci” (d).

Notice the distinction here between uppercase prefix symbols for the largest quantities and lowercase prefix symbols for the smallest quantities.

“J” represents joules (a unit of energy).

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